### 1. Information regarding the programme

| 1.1 Higher education  | Babeş Bolyai University                     |
|-----------------------|---|
| institution           |   |
| 1.2 Faculty           | Faculty of Mathematics and Computer Science |
| 1.3 Department        | Department of Mathematics                   |
| 1.4 Field of study    | Mathematics                                 |
| 1.5 Study cycle       | Master                                      |
| 1.6 Study programme / | Advanced Mathematics                        |
| Qualification         |   |

### 2. Information regarding the discipline

| 2.1 Name of the                                | e dis   | scipline | MN | IE3103 Group The | ory a | and applicati | ons        |
|--|---|----------|----|------------------|-------|---------------|------------|
| 2.2 Course coordinator prof. dr. Andrei Marcus |   |          |    |                  |       |               |            |
| 2.3 Seminar co                                 | 2.3 Seminar coordinator prof. dr. Andrei Marcus |          |    |                  |       |               |            |
| 2.4. Year of                                   | 1   | 2.5      | 2  | 2.6. Type of     | Ε     | 2.7 Type of   | Compulsory |
| study  |   | Semester |    | evaluation       |       | discipline    |            |

### 3. Total estimated time (hours/semester of didactic activities)

| 3.1 Hours per week  | 3  | Of which: 3.2 course | 2  | 3.3                            | 1     |
|---|----|----------------------|----|--------------------------------|-------|
|   |    |                      |    | seminar/l <del>aboratory</del> |       |
| 3.4 Total hours in the curriculum   | 42 | Of which: 3.5 course | 28 | 3.6                            | 14    |
|   |    |                      |    | seminar/ <del>laboratory</del> |       |
| Time allotment:   |    |                      |    |                                | hours |
| Learning using manual, course support, bibliography, course notes                     |    |                      |    |                                | 36    |
| Additional documentation (in libraries, on electronic platforms, field documentation) |    |                      |    |                                | 36    |
| Preparation for seminars/labs, homework, papers, portfolios and essays                |    |                      |    |                                | 36    |
| Tutorship   |    |                      |    |                                | 20    |
| Evaluations   |    |                      |    |                                | 30    |
| Other activities:   |    |                      |    |                                |       |
| 3.7 Total individual study hours 158  |    |                      |    |                                | •     |

| 3.7 Total mulvidual study nouis | 130 |
|---------------------------------|-----|
| 3.8 Total hours per semester    | 200 |
| 3.9 Number of ECTS credits      | 8   |

### 4. Prerequisites (if necessary)

| 4.1. curriculum   | - deep knowledge of bachelor level algebra, especially of the following subjects:    |
|-------------------|--|
|                   | - algebraic structures   |
|                   | - linear algebra   |
| 4.2. competencies | - ability to perform symbolic calculations ability to operate with abstract concepts |
|                   | - ability to do logical deductions   |
|                   | - ability to solve mathematics problems bases on aquired notions                     |

### **5. Conditions** (if necessary)

| 5.1. for the course       | • blackboard, projector |
|---------------------------|-------------------------|
| 5.2. for the seminar /lab | • blackboard            |
| activities                |                         |

# 6. Specific competencies acquired

| <b>Professional</b><br>competencies | <ul> <li>C1.1 Identifying the notions, describing the theories and using the specific language.</li> <li>C2.3 Applying the adequate analytical theoretical methods to a given problem.</li> </ul>  |
|-------------------------------------|--|
| Transversal<br>competencies         | • CT1. Applying some rules of precise and efficient work, showing a responsible attitude regarding the scientific domain and teaching training for an optimal and creative development of the personal potential in specific situations, respecting the deontological norms. |

## 7. Objectives of the discipline (outcome of the acquired competencies)

| 7.1 General objective of the discipline  | • Advanced knowledge on group theory. Ability to solve more difficult problems   |
|--|--|
| 7.2 Specific objective of the discipline | <ul> <li>students will operate with fundamental concepts of group theory</li> <li>students will aquire knowlegde regarding the structure of groups from various important classes.</li> <li>students solve problems, theoretical and practical, using instruments of modern algebra, regarding symmetry groups.</li> </ul> |

### 8. Content

| 8.1 Course   | Teaching methods                           | Remarks |
|--|--|---------|
| 1. Revision: groups, subgroups, factor group, isomorphism theorems. Symmetry groups.   | Explanation, dialogue,<br>examples, proofs |         |
| 2. The symmetric group. Group actions on sets.   | Explanation, dialogue,<br>examples, proofs |         |
| 3. p-groups and Sylow theorems   | Explanation, dialogue,<br>examples, proofs |         |
| 4. Direct and semidirect products. Finitely generated abelian groups. Dihedral groups. | Explanation, dialogue,<br>examples, proofs |         |
| 5. Group extensions. The Schur-Zassenhaus theorem.                                     | Explanation, dialogue,<br>examples, proofs |         |
| 6. Classification of groups of given order.  | Explanation, dialogue,<br>examples, proofs |         |
| 7. The general linear group.   | Explanation, dialogue,<br>examples, proofs |         |
| 8. Algebras, subalgebras, homomorphisms, ideals, factor algebras.                      | Explanation, dialogue,<br>examples, proofs |         |
| 9. Examples. Group algebra.  | Explanation, dialogue,<br>examples, proofs |         |

| 10. Representations and modules. Simple modules   | Explanation, dialogue, |
|---|------------------------|
| (irreducible representations) and                 | examples, proofs       |
| indecomposable modules.                           |                        |
| 11. Semisimple algebras and modules.              | Explanation, dialogue, |
|   | examples, proofs       |
| 12. Representations of finite groups. Characters. | Explanation, dialogue, |
|   | examples, proofs       |
| 13. Orthogonality of characters.                  | Explanation, dialogue, |
|   | examples, proofs       |
| 14. The character table of a finite group.        | Explanation, dialogue, |
|   | examples, proofs       |

Bibliography

[1] M.A. Armstrong. Groups and symmetry. Springer-Verlag 1988.

[2] J.J. Rotman. An introduction to the theory of groups. Springer-Verlag. 1995.

| 8.2 Seminar / laboratory                          | Teaching methods           | Remarks |
|---|----------------------------|---------|
| 15. Revision: groups, subgroups, factor group,    | dialogue, examples, proofs |         |
| isomorphism theorems. Symmetry groups.            |                            |         |
| 16. The symmetric group. Group actions on sets.   | dialogue, examples, proofs |         |
| 17. p-groups and Sylow theorems                   | dialogue, examples, proofs |         |
| 18. Direct and semidirect products. Finitely      | dialogue, examples, proofs |         |
| generated abelian groups. Dihedral groups.        |                            |         |
| 19. Group extensions. The Schur-Zassenhaus        | dialogue, examples, proofs |         |
| theorem.  |                            |         |
| 20. Classification of groups of given order.      | dialogue, examples, proofs |         |
| 21. The general linear group.                     | dialogue, examples, proofs |         |
| 22. Algebras, subalgebras, homomorphisms,         | dialogue, examples, proofs |         |
| ideals, factor algebras.                          |                            |         |
| 23. Examples. Group algebra.                      | dialogue, examples, proofs |         |
| 24. Representations and modules. Simple modules   | dialogue, examples, proofs |         |
| (irreducible representations) and                 |                            |         |
| indecomposable modules.                           |                            |         |
| 25. Semisimple algebras and modules.              | dialogue, examples, proofs |         |
| 26. Representations of finite groups. Characters. | dialogue, examples, proofs |         |
| 27. Orthogonality of characters.                  | dialogue, examples, proofs |         |
| 28. The character table of a finite group.        | dialogue, examples, proofs |         |
|   |                            |         |

Bibliography

3. J.L. Alperin and R.B. Bell. Groups and representatons. Springer-Verlag. 1995.

4. D.J.S. Robinson. An introduction to the theory of groups. 2nd Ed. Springer-Verlag. 1996.

5. B.E. Sagan. The symmetric group. Springer-Verlag. 2001.

6. John B. Fraleigh. A First course in abstract algebra. 6th edition, Addison Wesley.

7. Michael Artin. Algebra. Prentice Hall 1991.

- 8. D.S. Dummit and R.M. Foote. Abstract Algebra. 2nd edition. John Wiley & Sons, 1999.
- 9. J.A. Gallian. Contemporary Abstract Algebra. 7th Edition.

# **9.** Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

- Such a course exists in the curricula of all major universities in Romania and abroad;
- Groups are fundamental mathematical structures and have multiple applications in geometry,

#### 10. Evaluation

| Type of activity                    | 10.1 Evaluation criteria   | 10.2 Evaluation methods | 10.3 Share in the grade (%) |  |  |  |
|-------------------------------------|--|-------------------------|-----------------------------|--|--|--|
| 10.4 Course                         | <ul><li> know the basic principles<br/>of the field;</li><li> apply the new concepts</li></ul> | - written exam          | 75%                         |  |  |  |
| 10.5 Seminar/lab activities         | - problem solving  | - homeworks             | 25%                         |  |  |  |
| 10.6 Minimum performance standards  |  |                         |                             |  |  |  |
| to aquire 5 points to pass the exam |  |                         |                             |  |  |  |

| Date             | Signature of course coordinator | Signature of seminar coordinator    |
|------------------|---------------------------------|-------------------------------------|
| 17.04.2024       | Prof.dr. Andrei Mărcuș          | Prof.dr. Andrei Mărcuș              |
| Date of approval |                                 | Signature of the head of department |

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Prof.dr. Andrei Mărcuș