

SYLLABUS

1. Information regarding the programme

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|-------------------------------------|----------------------------------------------------|
| 1.1 Higher education institution | Babeş-Bolyai University |
| 1.2 Faculty | Faculty of Mathematics and Computer Science |
| 1.3 Department | Department of Computer Science |
| 1.4 Field of study | Computers and Information Technology |
| 1.5 Study cycle | Undergraduate |
| 1.6 Study programme / Qualification | Information Engineering |

2. Information regarding the discipline

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|---------------------------------|--------------------------------------------------------|--------------|----------|-------------------------|----------|------------------------|-------------------|
| 2.1 Name of the discipline (en) | Linear algebra, analytical and differential geometry 1 | | | | | | |
| (ro) | Algebra liniară, geometrie analitică și diferențială 1 | | | | | | |
| 2.2 Course coordinator | Assistant Professor PhD. Cosmin Pelea | | | | | | |
| 2.3 Seminar coordinator | Assistant Professor PhD. Cosmin Pelea | | | | | | |
| 2.4. Year of study | 1 | 2.5 Semester | 1 | 2.6. Type of evaluation | E | 2.7 Type of discipline | Compulsory |

3. Total estimated time (hours/semester of didactic activities)

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|---------------------------------------------------------------------------------------|-----|----------------------|----|------------------------|-------|
| 3.1 Hours per week | 4 | Of which: 3.2 course | 3 | 3.3 seminar/laboratory | 1 |
| 3.4 Total hours in the curriculum | 56 | Of which: 3.5 course | 42 | 3.6 seminar/laboratory | 14 |
| Time allotment: | | | | | hours |
| Learning using manual, course support, bibliography, course notes | | | | | 28 |
| Additional documentation (in libraries, on electronic platforms, field documentation) | | | | | 24 |
| Preparation for seminars/labs, homework, papers, portfolios and essays | | | | | 28 |
| Tutorship | | | | | 14 |
| Evaluations | | | | | 4 |
| Other activities: | | | | | - |
| 3.7 Total individual study hours | | 98 | | | |
| 3.8 Total hours per semester | 150 | | | | |
| 3.9 Number of ECTS credits | 6 | | | | |

4. Prerequisites (if necessary)

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| 4.1. curriculum | |
| 4.2. competencies | |

5. Conditions (if necessary)

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| 5.1. for the course | |
| 5.2. for the seminar /lab activities | |

6. Specific competencies acquired

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| Professional competencies | <p>C1.1 Identifying the notions, describing the theories and using the specific language</p> <p>C2.3 Applying the adequate analytical theoretical methods to a given problem.</p> |
| Transversal competencies | <p>CT1. Applying some rules of precise and efficient work, showing a responsible attitude regarding the scientific domain and teaching training for an optimal and creative development of the personal potential in specific situations, respecting the deontological norms.</p> |

7. Objectives of the discipline (outcome of the acquired competencies)

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| 7.1 General objective of the discipline | To introduce the basic notions of linear algebra. |
| 7.2 Specific objective of the discipline | To introduce some basic results on vector spaces, matrices, systems of linear equations, eigenvalues, eigenvectors and quadratic forms. |

8. Content

| 8.1 Course | Teaching methods | Remarks |
|--------------------------------|---------------------------------------------------------------------------------|---------|
| 1. Groups. Rings. Fields. | Interactive exposure Explanation Conversation Didactical demonstration | |
| 2. Matrix rings. Determinants. | Interactive exposure Explanation Conversation Didactical demonstration | |

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| 3. The rank of a matrix. The inverse of a matrix | Interactive exposure Explanation Conversation Didactical demonstration | |
| 4. Systems of linear equations | Interactive exposure Explanation Conversation Didactical demonstration | |
| 5. Elementary operations on a matrix. Applications | Interactive exposure Explanation Conversation Didactical demonstration | |
| 6. Vector spaces. Subspaces. The generated subspace | Interactive exposure Explanation Conversation Didactical demonstration | |
| 7. Linear maps | Interactive exposure Explanation Conversation Didactical demonstration | |
| 8. Test | | |
| 9. Linear independent vectors. Bases. The universal property of vector spaces. | Interactive exposure Explanation Conversation Didactical demonstration | |
| 10. The exchange theorem (Steinitz). Dimension. Dimension formulas | Interactive exposure Explanation Conversation Didactical demonstration | |
| 11. Matrices and linear maps | Interactive exposure Explanation Conversation Didactical demonstration | |
| 12. Eigenvectors and eigenvalues | Interactive exposure Explanation Conversation Didactical demonstration | |
| 13. Diagonalisable matrices. Hamilton-Cayley Theorem | Interactive exposure Explanation Conversation Didactical demonstration | |
| 14. Bilinear and quadratic forms. | Interactive exposure Explanation Conversation Didactical demonstration | |

Bibliography

1. R. COVACI, Algebra si programare liniara, Litografia UBB, Cluj-Napoca, 1986.
2. S. CRIVEI, Basic Abstract Algebra, Ed. Casa Cartii de Stiinta, Cluj-Napoca, 2002, 2003.
3. C. NASTASESCU, I. STANESCU, C. NITA, Matematica, Elemente de algebra superioara, Editura Didactica si Pedagogica, Bucuresti, 1995.
4. W. K. NICHOLSON, Linear Algebra and Applications, Lyryx Version,
https://lila1.lyryx.com/textbooks/OPEN_LAWA_1/marketing/Nicholson-OpenLAWA-2021A.pdf
5. I. PURDEA, I. POP, Algebra, Editura GIL, Zalau, 2003.

| 8.2 Seminar / laboratory | Teaching methods | Remarks |
|-----------------------------------|---------------------------------------------------------------------------------|---------|
| 1. Groups. Rings. Fields. Review. | Interactive exposure Explanation Conversation Didactical demonstration | |
| 2. Determinants. | Interactive exposure Explanation Conversation Didactical demonstration | |
| 3. The rank of a matrix | Interactive exposure Explanation Conversation Didactical demonstration | |
| 4. The inverse of a matrix | Interactive exposure Explanation Conversation Didactical demonstration | |
| 5. Systems of linear equations | Interactive exposure Explanation Conversation Didactical demonstration | |
| 6. Vector spaces. | Interactive exposure Explanation Conversation Didactical demonstration | |
| 7. Subspaces. Generated subspace | Interactive exposure Explanation Conversation Didactical demonstration | |
| 8. Linear maps | Interactive exposure Explanation Conversation Didactical demonstration | |
| 9. Bases | Interactive exposure Explanation Conversation Didactical demonstration | |

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| 10. Dimension formulas. | Interactive exposure Explanation Conversation Didactical demonstration | |
| 11. Dimension and generated subspaces. | Interactive exposure Explanation Conversation Didactical demonstration | |
| 12. Matrices and linear maps | Interactive exposure Explanation Conversation Didactical demonstration | |
| 13. Eigenvectors and eigenvalues. Diagonalisable matrices. Hamilton-Cayley Theorem | Interactive exposure Explanation Conversation Didactical demonstration | |
| 14. Bilinear and quadratic forms. | Interactive exposure Explanation Conversation Didactical demonstration | |

Bibliography

1. I.D. ION, N. RADU, Algebra (ed.4), Editura Didactica si Pedagogica, 1990.
2. I.D. ION, C. NITA, D. POPESCU, N. RADU: Probleme de algebra, Editura Didactica si Pedagogica, Bucuresti, 1981.
3. C. NASTASESCU, I. STANESCU, C. NITA, Matematica, Elemente de algebra superioara, Editura Didactica si Pedagogica, Bucuresti, 1995.
4. W. K. NICHOLSON, Linear Algebra and Applications, Lyryx Version,
https://lila1.lyryx.com/textbooks/OPEN_LAWA_1/marketing/Nicholson-OpenLAWA-2021A.pdf
5. I. PURDEA, C. PELEA, Probleme de algebra, EIKON, Cluj-Napoca, 2008.

9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

The course presents notions which often appear in other undergraduate courses. The course offers a sufficiently general background for some highschool algebra topics and the necessary tools to solve some specific problems.

10. Evaluation

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| 10.4 Course | Knowledge of basic concepts | Test | 25% |
| | Knowledge of basic results | Final exam. | 25% |
| 10.5 Seminar/laborator | Examples and problem solving | Final exam. | 50% |
| 10.6 Minimum performance standards | | | |

The final grade must be at least 5.

The required background for receiving the degree 5 contains:

- all the course notions;
- the statements of all the results presented in the course;
- the possibility to compute (any size) determinants, the inverse of a matrix, the rank of a matrix using all the algorithms discussed during the semester;
- the possibility to discuss the consistency and to solve systems of linear equations using all the algorithms discussed during the semester.

Date

23.04.2024

Signature of course coordinator

Assist. Prof. PhD. Cosmin Pelea

Signature of seminar coordinator

Assist. Prof. PhD. Cosmin Pelea

Date of approval

Signature of the head of department

Conf.PhD. Adrian-Ioan Sterca