#### **SYLLABUS**

## 1. Information regarding the programme

| 1.1 Higher education  | Babeş Bolyai University                     |
|-----------------------|---------------------------------------------|
| institution           |                                             |
| 1.2 Faculty           | Faculty of Mathematics and Computer Science |
| 1.3 Department        | Department of Computer Science              |
| 1.4 Field of study    | Computer Science                            |
| 1.5 Study cycle       | Master                                      |
|                       |                                             |
| 1.6 Study programme / | Applied Computational Intelligence          |
| Qualification         |                                             |

## 2. Information regarding the discipline

| 2.1 Name of the         | 2.1 Name of the discipline Mathematical Modeling |          |   |                                                   |  |  |  |  |
|-------------------------|--------------------------------------------------|----------|---|---------------------------------------------------|--|--|--|--|
| 2.2 Course coordinator  |                                                  |          |   | Assoc. Prof. PhD. Marcel-Adrian Şerban            |  |  |  |  |
| 2.3 Seminar coordinator |                                                  |          |   | Assoc. Prof. PhD. Marcel-Adrian Şerban            |  |  |  |  |
| 2.4. Year of            | 1                                                | 2.5      | 1 | 2.6. Type of <b>E</b> 2.7 Type of <b>Optional</b> |  |  |  |  |
| study                   |                                                  | Semester |   | evaluation discipline                             |  |  |  |  |
| 2.8 Course code MME3030 |                                                  |          |   |                                                   |  |  |  |  |
|                         |                                                  |          |   |                                                   |  |  |  |  |

# 3. Total estimated time (hours/semester of didactic activities)

| 3.1 Hours per week                                                                    | 4  | Of which: 3.2 course | 2  | 3.3                        | 1sem/ 1 |
|---------------------------------------------------------------------------------------|----|----------------------|----|----------------------------|---------|
|                                                                                       |    |                      |    | seminar/laboratory/project | pr      |
| 3.4 Total hours in the                                                                | 56 | Of which: 3.5 course | 28 | 3.6                        | 28      |
| curriculum                                                                            |    |                      |    | seminar/laboratory/project |         |
| Time allotment:                                                                       |    |                      |    |                            |         |
| Learning using manual, course support, bibliography, course notes                     |    |                      |    |                            | 16      |
| Additional documentation (in libraries, on electronic platforms, field documentation) |    |                      |    |                            | 18      |
| Preparation for seminars/labs, homework, papers, portfolios and essays                |    |                      |    |                            | 20      |
| Tutorship                                                                             |    |                      |    |                            | 20      |
| Evaluations                                                                           |    |                      |    |                            | 20      |
| Other activities:                                                                     |    |                      |    |                            | -       |
| 2777 4 1 1 1 1 1 4 1                                                                  | 1  | 0.4                  |    |                            | 1       |

| 3.7 Total individual study hours | 94  |
|----------------------------------|-----|
| 3.8 Total hours per semester     | 150 |
| 3.9 Number of ECTS credits       | 6   |

# **4. Prerequisites** (if necessary)

| 4.1. curriculum   |  |
|-------------------|--|
| 4.2. competencies |  |

# **5. Conditions** (if necessary)

| 5.1. for the course       | <ul> <li>basic knowledge in dynamical systems</li> </ul>                |
|---------------------------|-------------------------------------------------------------------------|
| 5.2. for the seminar /lab | <ul> <li>Laboratory with computers; basic knowledge in MAPLE</li> </ul> |
| activities                |                                                                         |

6. Specific competencies acquired

| Professional competencies ' | • | Knowledge, understanding and use of basic concepts of discrete and continuous dynamical systems  Ability to work independently and/or in a team in order to solve problems in defined professional contexts.  Good programming skills in MAPLE |
|-----------------------------|---|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Transversal competencies    | • | Ability to apply mathematical tools to different real life problems Ability to model phenomena using dynamical systems Improved modeling abilities: mathematical modelling, model analysis, numerical simulations                              |

# 7. Objectives of the discipline (outcome of the acquired competencies)

| 7.1 General objective of the discipline | <ul> <li>Be able to describe real world phenomena in mathematical language</li> <li>Improved modeling abilities: mathematical modelling, model analys</li> </ul> |  |
|-----------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|
|                                         | numerical simulations                                                                                                                                            |  |
| 7.2 Specific objective of the           | Acquire knowledge about discrete and continuous dynamical systems                                                                                                |  |
| discipline                              | Apply discrete and continuous dynamical systems in mathematical                                                                                                  |  |
|                                         | modelling of real world phenomena                                                                                                                                |  |
|                                         | Understand and work with mathematical models                                                                                                                     |  |

### 8. Content

| 8.1 Course                                    | Teaching methods           | Remarks |
|-----------------------------------------------|----------------------------|---------|
| 1. Mathematical Models. Modelling Change with | Exposure: description,     |         |
| Difference Equations                          | explanation, examples,     |         |
|                                               | discussion of case studies |         |
| 2. Difference Equations. Equilibrium Points.  | Exposure: description,     |         |
| Periodic Points                               | explanation, examples,     |         |
|                                               | discussion of case studies |         |
| 3. Solving Difference Equations with MAPLE    | Exposure: description,     |         |
|                                               | explanation, examples,     |         |
|                                               | debate, dialogue           |         |
| 4. Stability of the Equilibrium Points.       | Exposure: description,     |         |
| Mathematical Models Given by Difference       | explanation, examples,     |         |
| Equations                                     | discussion of case studies |         |
| 5. Solving Differential Equations with MAPLE  | Exposure: description,     |         |
|                                               | explanation, examples,     |         |
|                                               | proofs                     |         |
| 6. Approximating Solutions of Differential    | Exposure: description,     |         |
| Equations                                     | explanation, examples,     |         |
|                                               | proofs, debate, dialogue   |         |
| 7. Modelling with First Order Differential    | Exposure: description,     |         |
| Equations                                     | explanation, examples,     |         |
|                                               | discussion of case studies |         |
| 8. Mathematical Models in One Population      | Exposure: description,     |         |
| Dynamics                                      | explanation, examples      |         |
| 9. Mathematical Models for Interacting        | Exposure: description,     |         |
| Populations                                   | explanation, examples      |         |

|                                                 | discussion of case studies |
|-------------------------------------------------|----------------------------|
| 10. Modelling with Second Order Differential    | Exposure: description,     |
| Equations                                       | explanation, examples,     |
|                                                 | debate                     |
| 11. Vertical Stabilization of a Rocket on a     | Exposure: description,     |
| Movable Platform                                | explanation, discussion    |
|                                                 | of case studies            |
| 12. A Suspension Bridge Model                   | Exposure: description,     |
|                                                 | explanation, discussion    |
|                                                 | of case studies            |
| 13. Chaos Theory: Chaotic Discrete-Time Models, | Exposure: description,     |
| the Discrete Logistical Model                   | explanation, examples,     |
|                                                 | discussion of case studies |
| 14. Chaos Theory: Chaotic Continuous-Time       | Exposure: description,     |
| Models, the Loretnz Model                       | examples, discussion of    |
|                                                 | case studies, live demo    |

#### Bibliography

- 1. I.A.Rus, C. Iancu, Mathematical modeling, Transilvania Press, 2000.
- 2. F.R. Giordano, M.D. Weir, W.P. Fox, A first course in mathematical modeling, Brooks/Coole, 2003.
- 3. D.K. Arrowsmith, Dynamical systems, Differential equations, maps and chaotic behaviour, Chapmann and Hall, 1992.
- 4. Lynch S. Dynamical systems with applications using MAPLE, Birkhauser, 2001.
- 5. Ronald W. Shonkwiler, Mathematical Biology. An Introduction with Maple and Matlab, Springer, 2009.
- 6. J.D. Murray, Mathematical biology, Springer, 2001.

| 8.2 Seminar                                  | Teaching methods          | Remarks |
|----------------------------------------------|---------------------------|---------|
| Solving difference equations with MAPLE      | Explation, dialogue, case |         |
|                                              | studies                   |         |
| 2. Stability of the Equilibrium Points for   | Dialogue, debate, case    |         |
| Diference Equations. Case Studies with       | studies, examples, proofs |         |
| MAPLE                                        |                           |         |
| 3. Mathematical Models Given by Difference   | Dialogue, debate, case    |         |
| Equations                                    | studies, examples, proofs |         |
| 4. Solving Differential Equations with MAPLE | Dialogue, debate, case    |         |
|                                              | studies, examples         |         |
| 5. Modelling with First Order Differential   | Dialogue, debate, case    |         |
| Equations                                    | studies, examples         |         |
| 6. Modelling with Second Order Differential  | Dialogue, debate, case    |         |
| Equations                                    | studies, examples         |         |
| 7. Mathematical Models for Interacting       | Dialogue, debate, case    |         |
| Populations                                  | studies, examples         |         |

#### Bibliography

- 1. F.R. Giordano, M.D. Weir, W.P. Fox, A first course in mathematical modeling, Brooks/Coole, 2003.
- 2. D.K. Arrowsmith, Dynamical systems, Differential equations, maps and chaotic behaviour, Chapmann and Hall, 1992.

| 3. Lynch S. Dynamical systems with applications using MAPLE, Birkhauser, 2001.                        |                  |         |  |  |  |
|-------------------------------------------------------------------------------------------------------|------------------|---------|--|--|--|
| 4. Ronald W. Shonkwiler, Mathematical Biology. An Introduction with Maple and Matlab, Springer, 2009. |                  |         |  |  |  |
| 8.3 Laboratory                                                                                        | Teaching methods | Remarks |  |  |  |
|                                                                                                       |                  |         |  |  |  |
|                                                                                                       |                  |         |  |  |  |

# 9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

- The course respects the IEEE and ACM Curricula Recommendations for Computer Science studies;
- The course exists in the studying program of all major universities in Romania and abroad;

#### 10. Evaluation

| Type of activity                                                                   | 10.1 Evaluation criteria                                                                                                                 | 10.2 Evaluation methods                            | 10.3 Share in the grade (%) |  |
|------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------|-----------------------------|--|
| 10.4 Course                                                                        | <ul><li>know the basic principle of the domain;</li><li>apply the course concepts</li><li>problem solving</li></ul>                      | Written exam                                       | 70%                         |  |
| 10.5 Seminar/lab activities                                                        | <ul><li>be able to implement<br/>course concepts</li><li>apply techniques for<br/>different classes of<br/>mathematical models</li></ul> | -Practical examination<br>-continuous observations | 30%                         |  |
| 10.6 Minimum performance standards                                                 |                                                                                                                                          |                                                    |                             |  |
| At least grade 5 (from a scale of 1 to 10) at both written exam and seminary work. |                                                                                                                                          |                                                    |                             |  |

| Date             | Signature of course coordinator        | Signature of seminar coordinator       |  |
|------------------|----------------------------------------|----------------------------------------|--|
| 30.04.2024       | Assoc. Prof. PhD. Marcel-Adrian ŞERBAN | Assoc. Prof. PhD. Marcel-Adrian ŞERBAN |  |
|                  |                                        |                                        |  |
|                  |                                        |                                        |  |
| Date of approval |                                        | Signature of the head of department    |  |
|                  |                                        | Prof PhD Andrei Marcus                 |  |