#### **SYLLABUS**

## 1. Information regarding the programme

1.1 Higher education	Babeş-Bolyai University
institution	
1.2 Faculty	Faculty of Mathematics and Computer Science
1.3 Department	Department of Computer Science
1.4 Field of study	Computers and Information Technology
1.5 Study cycle	Bachelor
1.6 Study programme /	Information Engineering
Qualification	

## 2. Information regarding the discipline

2.1 Name of the discipline Calculus 1/							
			Analiză matematică 1				
2.2 Course coo	rdi	nator	Lect. dr. GRAD ANCA				
2.3 Seminar co	ord	inator	Lect. dr. GRAD ANCA				
2.4. Year of	1	2.5	1	2.6. Type of Written 2.7 Type of Compulsory			
study		Semester		evaluation	exam	discipline	DF

## **3. Total estimated time** (hours/semester of didactic activities)

3.1 Hours per week	5	Of which: 3.2 course	3	3.3	2 S
				seminar/laboratory	
3.4 Total hours in the curriculum	70	Of which: 3.5 course	42	3.6	28
				seminar/laboratory	
Time allotment:					
Learning using manual, course support, bibliography, course notes					
Additional documentation (in libraries, on electronic platforms, field documentation)					
Preparation for seminars/labs, homework, papers, portfolios and essays					25
Tutorship					10
Evaluations					10
Other activities:					

3.7 Total individual study hours	80
3.8 Total hours per semester	150
3.9 Number of ECTS credits	6

## **4. Prerequisites** (if necessary)

4.1. curriculum	High-school calculus
4.2. competencies	Mathematical thinking, logical thinking

## **5. Conditions** (if necessary)

5.1. for the course	Lecture hall with large board and beamer
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# 6. Specific competencies acquired

Professional competencies	C1.1 Recognizing and describing specific concepts to calculability, complexity, programming paradigms and modelling of computing and communication systems  C1.2 Using specific theories and tools (algorithms, schemes, models, protocols, etc.) for explaining the structure and the functioning of hardware, software and communication systems  C1.3 Building models for various components of computing systems  C1.4 Formal evaluation of the functional and non-functional characteristics of computing systems  C1.5 Providing theoretical background for the characteristics of the designed systems
Transversal competencies	CT1 Application of efficient and rigorous working rules, manifest responsible attitudes towards the scientific and didactic field, respecting the professional and ethical principles.  CT3 Use of efficient methods and techniques for learning, information, research and development of abilities for knowledge acquiring, for adapting to the needs of dynamic society and for communication in Romanian as well as in a widely used foreign language.

## **7. Objectives of the discipline** (outcome of the acquired competencies)

7.1 General objective of the discipline	Acquiring knowledge about the algebraic and topological structure of the space R, differential and integral calculus
7.2 Specific objective of the discipline	<ul> <li>Presentation of the basic notions and concepts connected to the topology of R</li> <li>Presentation of the basic notoions and results concerning sequences and series of real numbers</li> <li>Presentation of the basic notions and results concerning the differential and integral calulus of real functions of one real variable</li> </ul>

#### 8. Content

8.1 Course	Teaching methods	Remarks
1. The system of real numbers (upper and lower	Lecture, discussion,	[1] pp. 125-157
bound of a set; minimum and maximum of a set;	didactic proofs	or
infimum and supremum of a set; the infimum	1	[4] pp. 80-97
principle, the supremum principle and its		[1] pp. 66 77
consequences; the sets of natural numbers, the set		
integer numbers, the set of rational numbers, and the		
set of irrational numbers; the extended set of real		
numbers). Topology of the real axis (neighbourhoods,		
open sets, interior set, exterior set, boundary set,		
closure, accumulation points)		
<b>2.</b> Sequences of real numbers (existence of the limit for	Lecture, discussion,	[4] pp. 159-195, 259-263
monotone sequences; applications: the irrational number		

e)	didactic proofs	
3. Fundamental sequences. Series of real numbers (convergence/divergence criteria for series: Cauchy's general criterion, Cauchy's condensation criterion, comparison criteria, the root criterion, Kummer's, D'Alembert's and Raabe-Duhamel's criteria)	Lecture, discussion, didactic proofs	[4] pp. 313-346
4. Series of real numbers; comparison criteria.	Lecture, discussion, didactic proofs	[4] pp. 367-396
<b>5.</b> Series of real numbers (Abel-Dirichlet criterion; absolutely convergent series; the Leibniz criterion for alternant series; convolutive product of series).	Lecture, discussion, didactic proofs	[2], pp. 193 – 204 pp. 232 – 244 [6], pp. 290 – 298 pp. 348 – 353
<b>6.</b> Limits of real-valued functions, characterization theorems. Continuous functions, characterization theorems.	Lecture, discussion, didactic proofs	[4] pp.
7. Differential calculus. Mean theorems	Lecture, discussion, didactic proofs	[1] pp. 195-232 or [4] pp. 409-420, 459- 472, 486-507
<b>8.</b> Higher order derivatives; Taylor's theorem and applications.	Lecture, discussion, didactic proofs	[1] pp. 233-263 or [4] pag. 579-594
<b>9.</b> Sequences of functions (convergence and uniform convergence; properties of the sum function).	Lecture, discussion, didactic proofs	[4], pp. 427 – 441
10. Series of functions (convergence and uniform convergence; properties of the sum function).  Power series. Taylor's theorem	Lecture, discussion, didactic proofs	[4], pp. 361 – 365 pp. 441 – 445
<b>11.</b> The Riemann integral (definition, characterizations of inerrability; properties of the Riemann integral)	Lecture, discussion, didactic proofs	[4], pp. 365 – 384
12 Primitives, the Leibniz-Newton formula.	Lecture, discussion, didactic proofs	[1] pp. 314-388
13. Improper integrals	Lecture, discussion, didactic proofs	[4], pp. 379-391
14. The Riemann-Stieltejes integral	Lecture, discussion, didactic proofs	[7], pp. 221 – 240

Bibliography

- 1. D. Andrica, D.I. Duca, I. Purdea, I. Pop: Matematica de baza, Editura Studium, Cluj-Napoca, 2004
- 2. W.W. Breckner: Analiza matematica. Topologia spatiului R^n, Universitatea din Cluj-Napoca, Cluj -Napoca, 1985
- 3. S. Cobzas: Analiza matematica (Calcul diferential), Presa Universitara Clujeana, Cluj-Napoca, 1997
- 4. D.I. Duca: Analiza matematica (vol. I), Casa Cartii de Stiinta, Cluj-Napoca, 2013
- 5. D.I. Duca, E. Duca: Exercitii si probleme de analiza matematica (vol. I), Editura Casa Cartii de Stiinta, Cluj-Napoca, 2007
- 6. D.I. Duca, E. Duca: Exercitii si probleme de analiza matematica (vol II), Editura Casa Cartii de Stiinta, Cluj
- -Napoca, 2009
- 7. M. Megan: Bazele Analizei matematice, vol. 1,2,3, Editura Eurobit, 1997, 1997, 1998
- 8. Gh. Siretchi: Calcul diferential si integral, vol. I si II, Editura Stiintifica si Enciclopedica, Bucuresti, 1985
- 9. V.A. Zorich: Mathematical Analysis, Springer, Berlin, 2004

8.2 Seminar / laboratory	Teaching methods	Remarks
<b>1.</b> The set of real numbers. Topology of the set of real numbers.	Discussions, problematisation, self-tanking, team- work	[5] 1.2-1.4; 1.7-1.10; 1.12- 1.16; 2.2; 2.4-2.6; 2. 8-2.9; 2.11-2.32
2. Real number sequences; convergence of the monotone sequences.	Discussions, problematisation, self-tanking, team- work	[5] 3.24; 3.26; 3.33; 3.39; 3. 43; 3.47; 3.54; 3.59; 3.67- 3.73; 3.85; 3.90; 3.95; 3.99- 3.108
3. Fundamental sequences. Series of real numbers.	Discussions, problematisation, self-thinking, teamwork	List of problems edited by the lecturer
<b>4.</b> Series of real numbers.	Discussions, problematisation, self-thinking, team- work	List of problems edited by the lecturer
<ol><li>Limits of functions. Continuous functions</li></ol>	Discussions, problematisation, self-thinking, team- work	[5] 4.2-4.3; 4.7; 4.12; 4.16; 4.18; 4.22; 4.24-4.26; 4.41; 4.45; 4.47; 4.50; 4.56; 4.73- 4.75; 4.79; 4.80; 4.84; 4.94 5.2; 5.8; 5.11; 5.15-5.19; 5.22; 5.26; 5.29; 5.31; 5.35; 5.40; 5.41
<b>6.</b> Limits of real-valued functions, characterization theorems. Continuous functions, characterization theorems.	Discussions, problematisation, self-thinking, team- work	[3] 6.2; 6.14-6.17; 6.21; 6.26-6.32; 6.92-6.95; 7.10; 7.12-7.17; 7.24-7.36; 7.48; 7.52; 7.57-7.63
7. Differential calculus. Mean theorems	Discussions, problematisation, self-thinking, team- work	[3] 6.68-6.90; 6.169-6.187
8. Higher order derivatives; Taylor's theorem and applications.	Discussions, problematisation, self-thinking, team- work	[4] 1.2; 1.14; 1.20; 1.22; 1.32; 1.39-1.40; 1.65-1.66; 1.126; 2.6-2.42; 2.46-2.51; 2.60; 2.68; 2.72-2.74; 2.78; 2.82-2.89; 2.130-2.131; 2.139; 2.147; 2.171; 2.224; 2.262; 2.303; 2.307; 2.314
<b>9.</b> Sequences of functions (convergence and uniform convergence; properties of the sum function).	Discussions, problematisation, self-thinking, team- work	[1] pp. 339-352
10. Series of functions (convergence and uniform convergence; properties of the sum function). Power series. Taylor's theorem	Discussions, problematisation, self-thinking, team-	List of problems edited by the lecturer

	work	
11. The Riemann integral (definition, characterizations	Discussions,	[1] pag. 277-313
of inerrability; properties of the Riemann integral)	problematisation,	
	self-thinking, team-	
	work	
12 Primitives, the Leibniz-Newton formula.	Discussions,	[1] pag. 314-338
	problematisation,	
	self-thinking, team-	
	work	
	Discussions,	[8] pag. 379-391
	problematisation,	
13. Improper integrals	self-thinking, team-	
200 200pt open 200gt 100	work	
	Discussions,	[7] pp. 221-240
	problematisation,	
	self-thinking, team-	
14. The Riemann-Stieltejes integral	work	

# 9. Corroborating the content of the discipline with the expectations of the epistemic community, professional associations and representative employers within the field of the program

The content of this course can be encountered in the syllabus of every respected university in land or abroad. It represents a basic foundation not only for each student which is interested in fixed sciences. It is imperative for the study of optimization, mathematical modelling, partial equations, statistics, probability and many other domains.

#### 10. Evaluation

10. Evaluation			
Type of activity	10.1 Evaluation criteria	10.2 Evaluation methods	10.3 Share in the grade (%)
10.4 Course	knowledge of the basic notions and results knowledge of the proofs for	Final written exam	60%
	the main theoretical results		
10.5 Seminar/lab activities	Homework including problems based on the theory presented at the lecture	Continuous evaluation during the seminar	20%
	application of the theroretical results to practical problems	written quizzes during the seminar	20%
10.6 Minimum performance standards			

➤ The definitions, the statement of the theoretical results and straight-forward applications

> Idenfitication and proper selection of the solving methods for various practical problems

Date Signature of course coordinator

Signature of seminar coordinator

09.05.2023 Lect. dr. GRAD ANCA

Lect. dr. GRAD ANCA

Prof. dr. Laura Dioșan

24.05.2022

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